

# Introduction to EEG and MEG source modelling

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# Outline

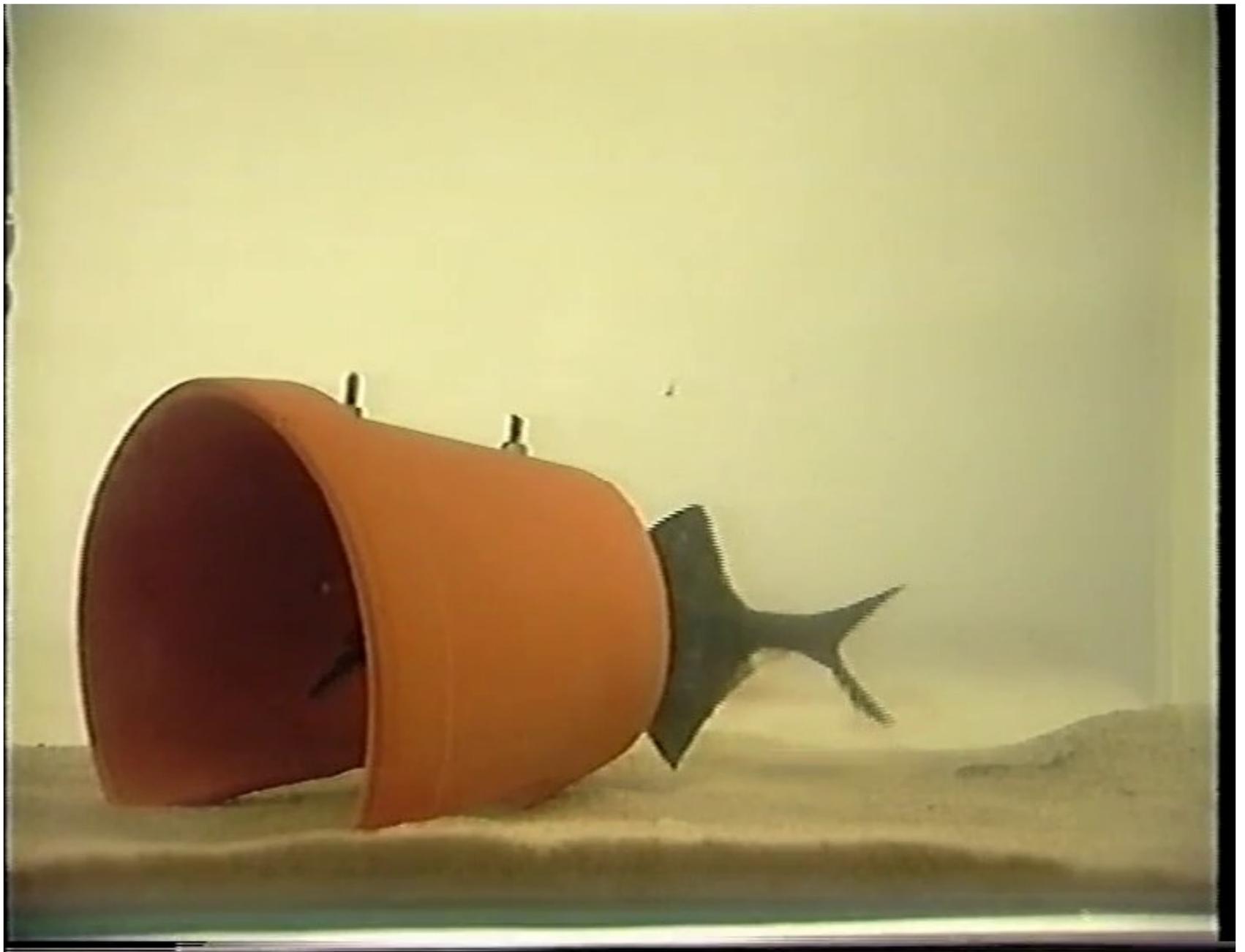
Motivation

Source and volume conduction models  
using anatomical information  
aligning sensors with anatomy

Source reconstruction

equivalent dipole fitting  
distributed models  
scanning methods

Summary



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## **Motivation**

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# Motivation 1

## Strong points of EEG and MEG

- Temporal resolution ( $\sim 1$  ms)

- Characterize individual components of ERP

- Oscillatory activity

- Disentangle dynamics of cortical networks

## Weak points of EEG and MEG

- Measurement on outside of brain

- Overlap of components

- Low spatial resolution

## Motivation 2

If you find a ERP/ERF component, you want to characterize it in physiological terms

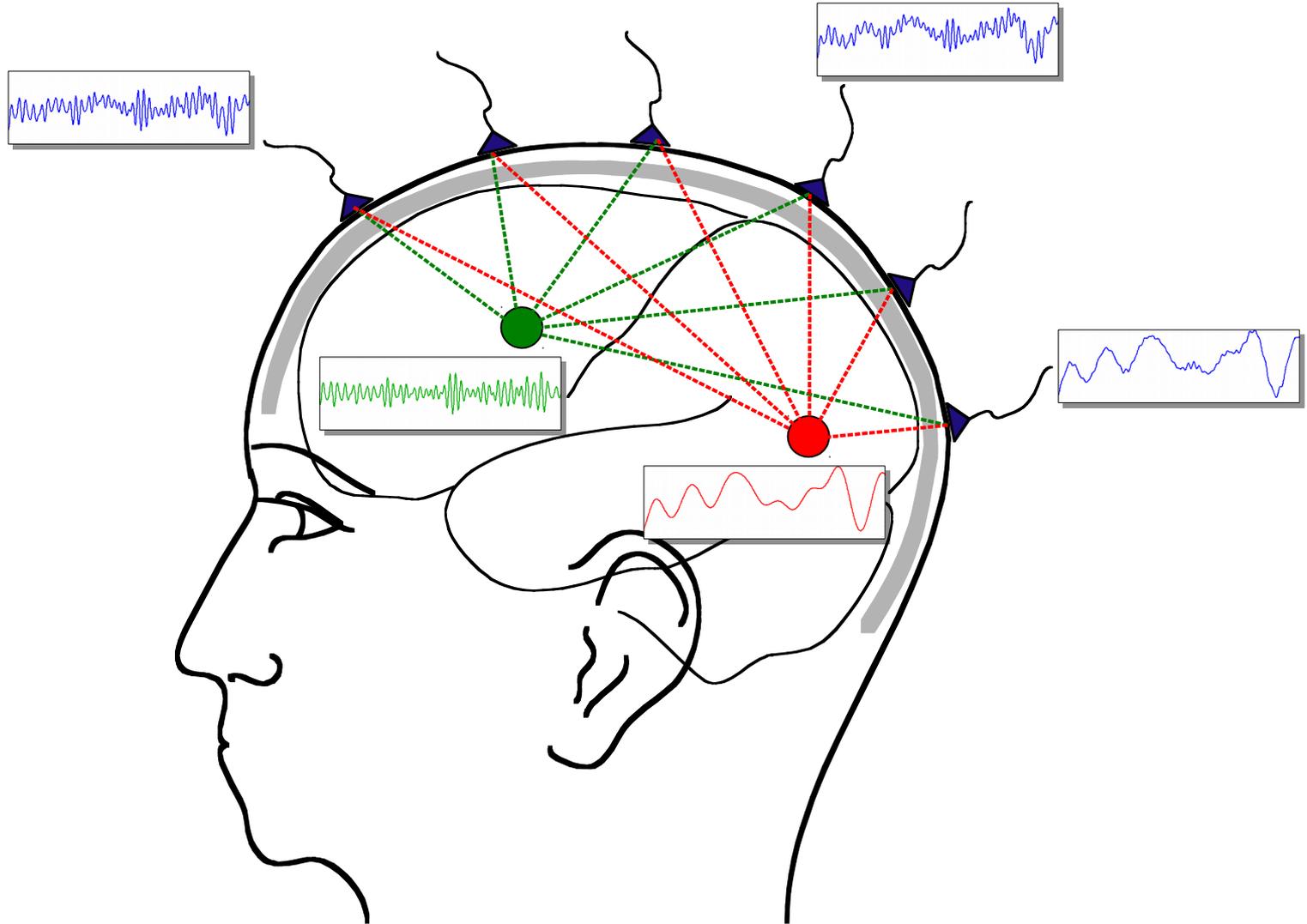
Time or frequency are the “natural” characteristics

“Location” requires interpretation of the scalp topography

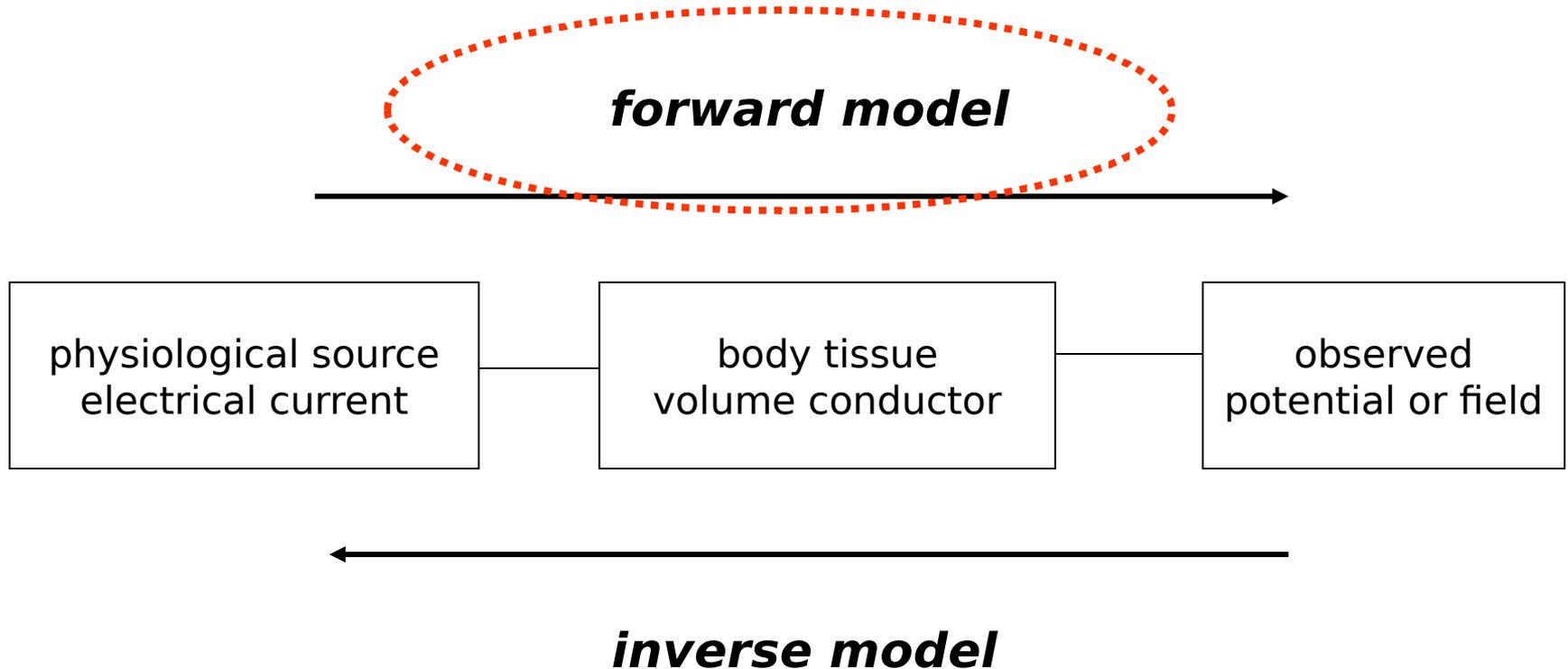
Forward and inverse modelling helps to interpret the topography

Forward and inverse modelling helps to disentangle overlapping source timeseries

# Superposition of source activity



# Biophysical source modelling: overview



# Outline

Motivation

## **Source and volume conduction models**

using anatomical information

aligning sensors with anatomy

Source reconstruction

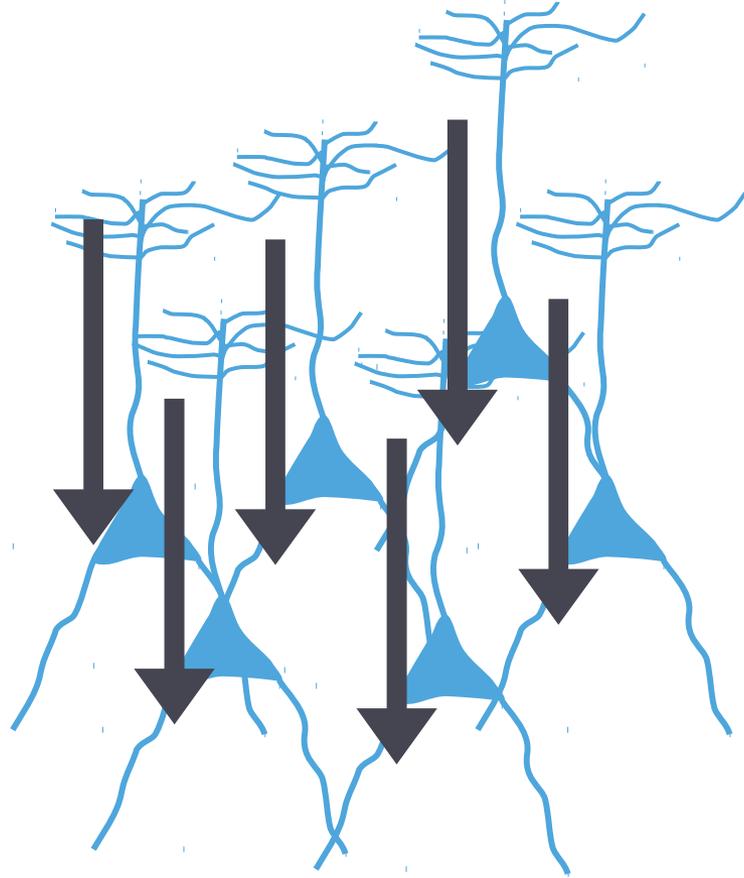
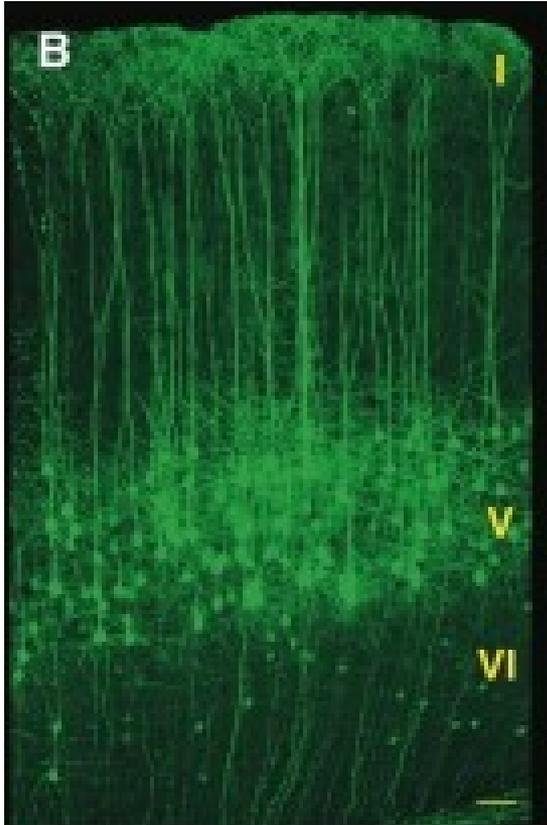
equivalent dipole fitting

distributed models

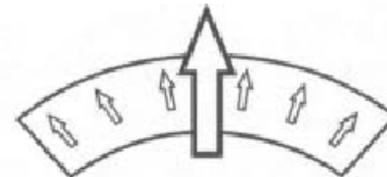
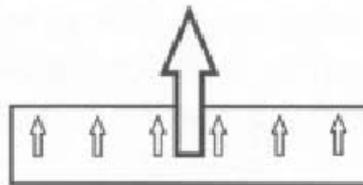
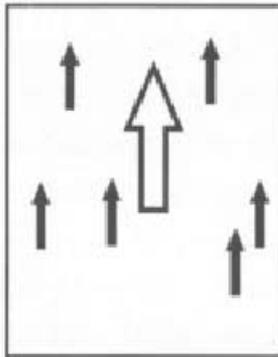
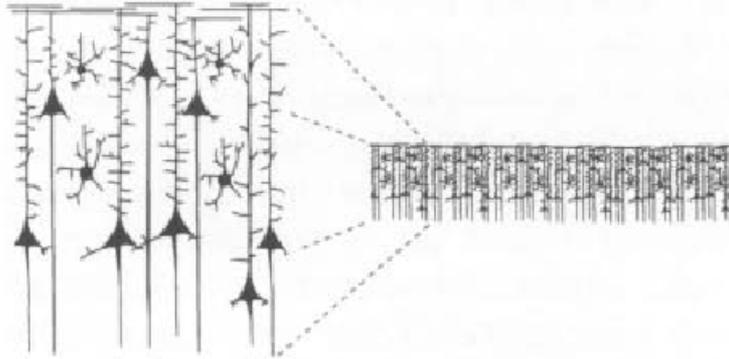
scanning methods

Summary

What produces the electric current



# Equivalent current dipoles



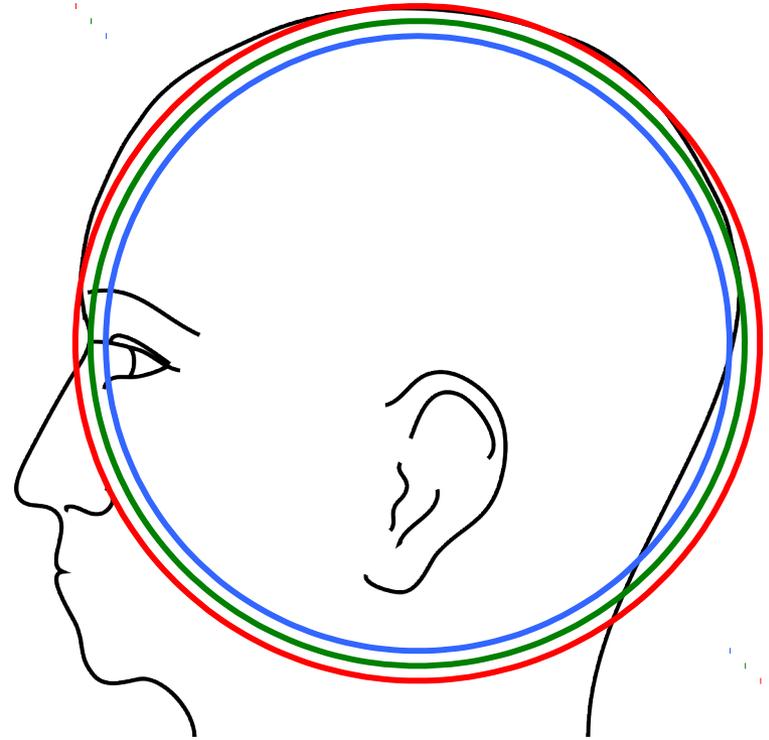
# Volume conductor

described electrical properties of tissue

describes geometrical model of the head

describes **how** the currents flow, not where they originate from

same volume conductor for EEG as for MEG, but also for tDCS, tACS, TMS, ...



# Volume conductor

Computational methods for volume conduction problem that allow for realistic geometries

BEM *Boundary Element Method*

FEM *Finite Element Method*

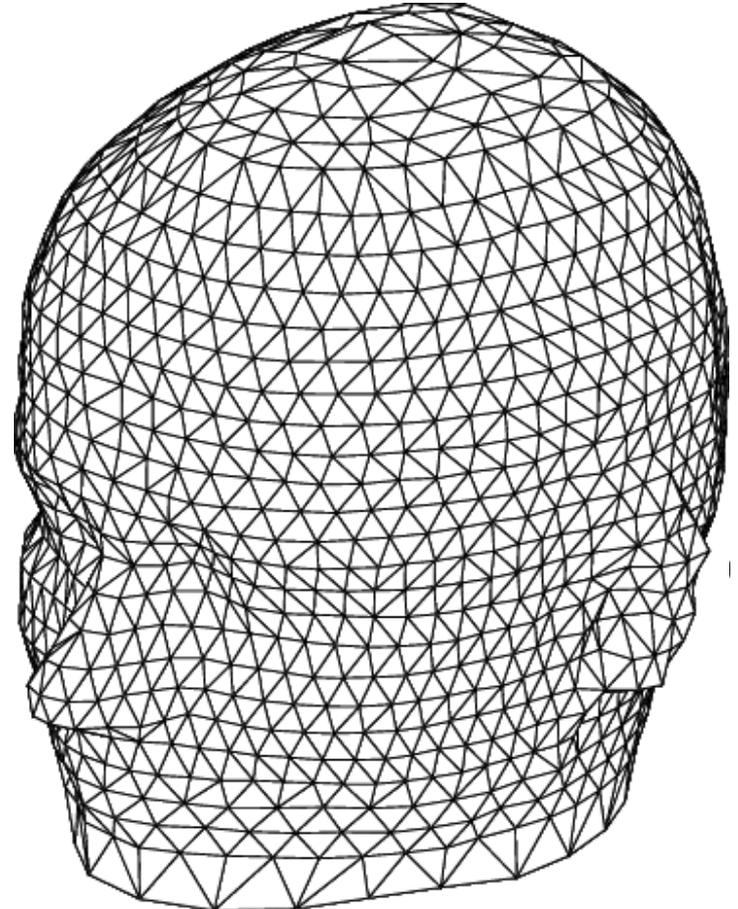
FDM *Finite Difference Method*

# Volume conductor: Boundary Element Method

Each compartment is  
homogenous  
isotropic

Important tissues  
skin  
skull  
brain  
(CSF)

Triangulated surfaces  
describe boundaries



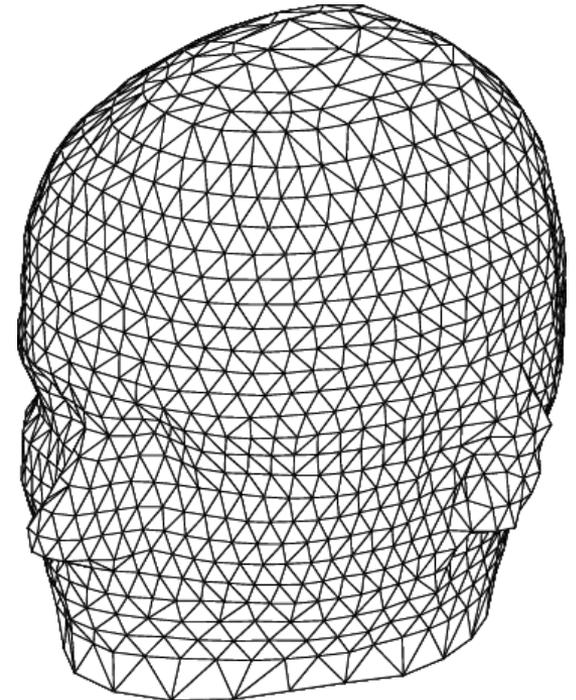
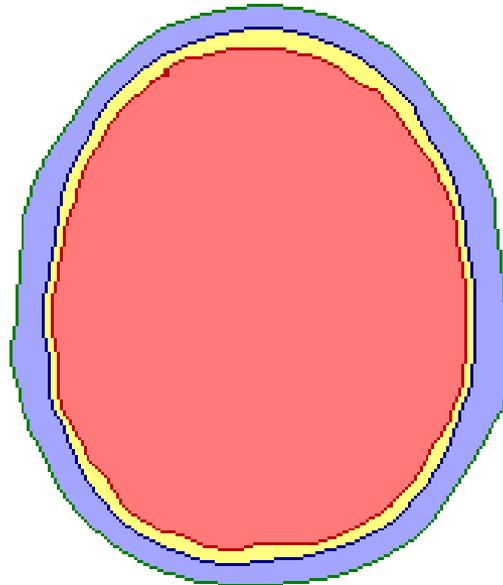
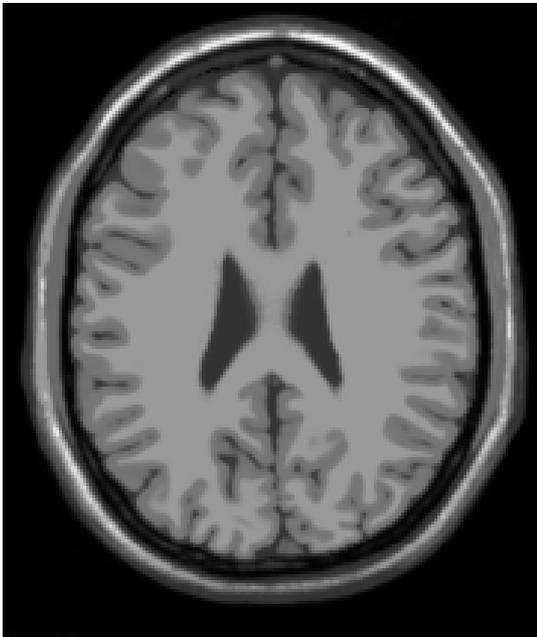
# Volume conductor: Boundary Element Method

## Construction of geometry

segmentation in different tissue types

extract surface description

downsample to reasonable number of triangles



# Volume conductor: Boundary Element Method

## Construction of geometry

- segmentation in different tissue types

- extract surface description

- downsample to reasonable number of triangles

## Computation of model

- independent of source model

- only one lengthy computation

- fast during application to real data

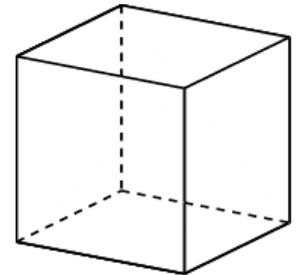
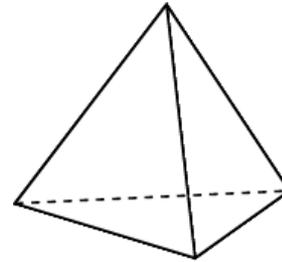
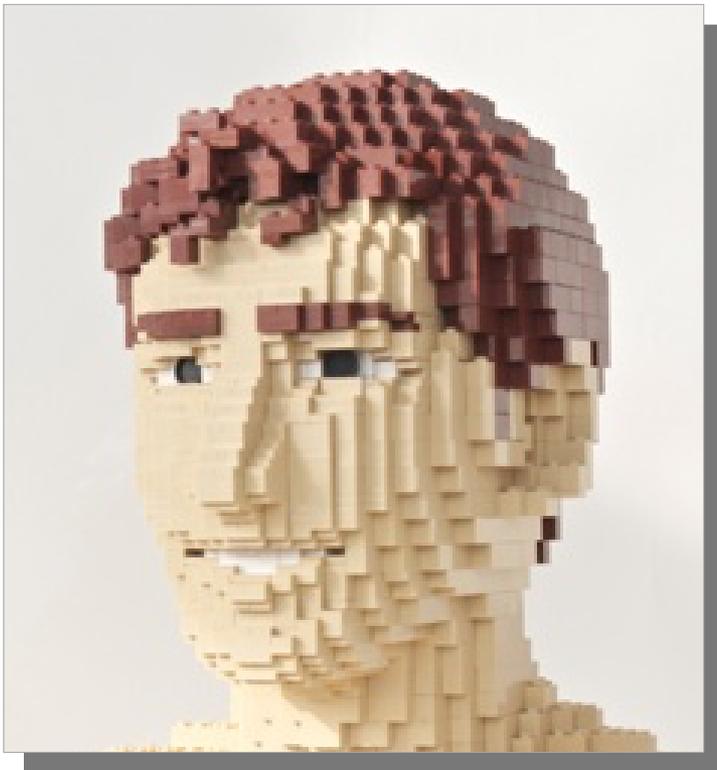
## Can also include more complex geometrical details

- ventricles

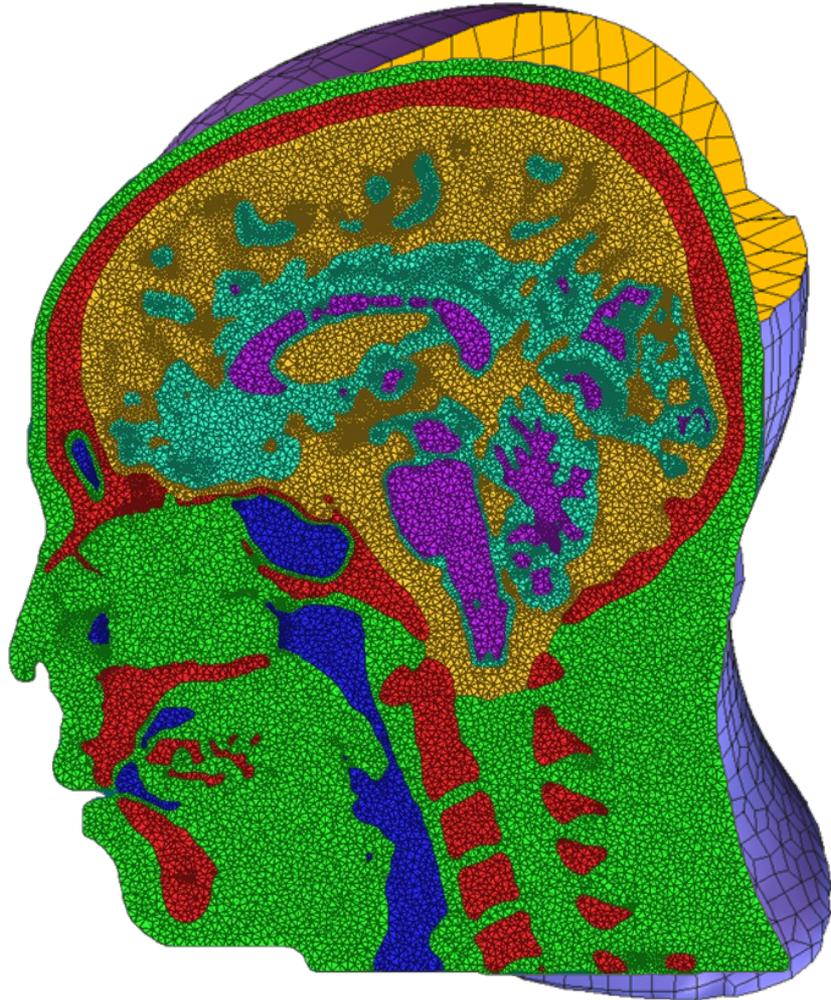
- holes in skull

# Volume conductor: Finite Element Method

Tessellation of 3D volume in tetraeders or hexaheders



# Volume conductor: Finite Element Method

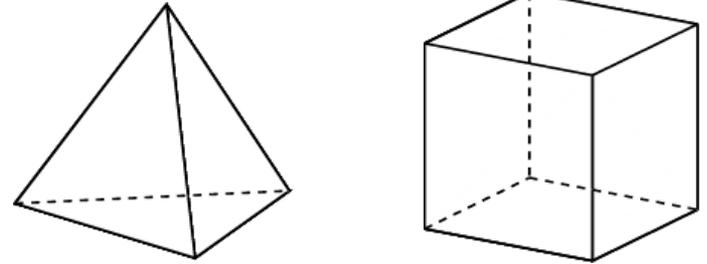


tetraeders

hexaheders

# Volume conductor: Finite Element Method

Tessellation of 3D volume in tetraeders or hexaheders



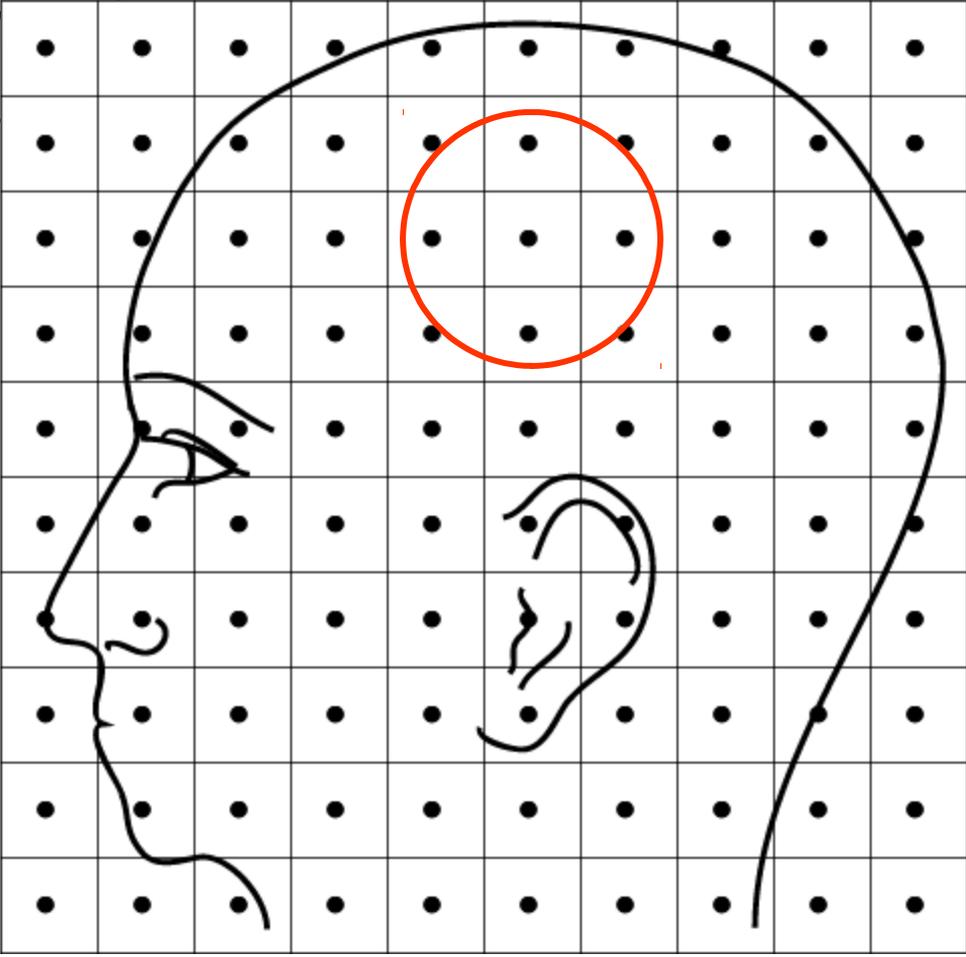
Each element can have its own conductivity

FEM is the most accurate numerical method but computationally quite expensive

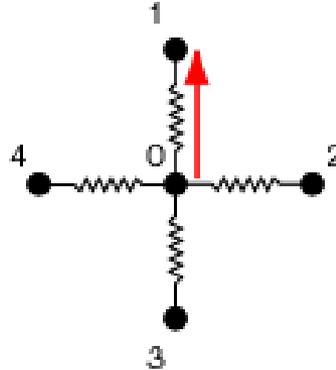
Geometrical processing not as simple as BEM

# Volume conductor: Finite Difference Method

Easy to con  
Not very us



# Volume conductor: Finite Difference Method



$$\left. \begin{aligned} I_1 + I_2 + I_3 + I_4 &= 0 \\ V &= I * R \end{aligned} \right\} \Rightarrow$$

$$\Delta V_1 / R_1 + \Delta V_2 / R_2 + \Delta V_3 / R_3 + \Delta V_4 / R_4 = 0 \quad \Rightarrow$$

$$(V_1 - V_0) / R_1 + (V_2 - V_0) / R_2 + (V_3 - V_0) / R_3 + (V_4 - V_0) / R_4 = 0$$

# Volume conductor: Finite Difference Method

Unknown potential  $V_i$  at each node

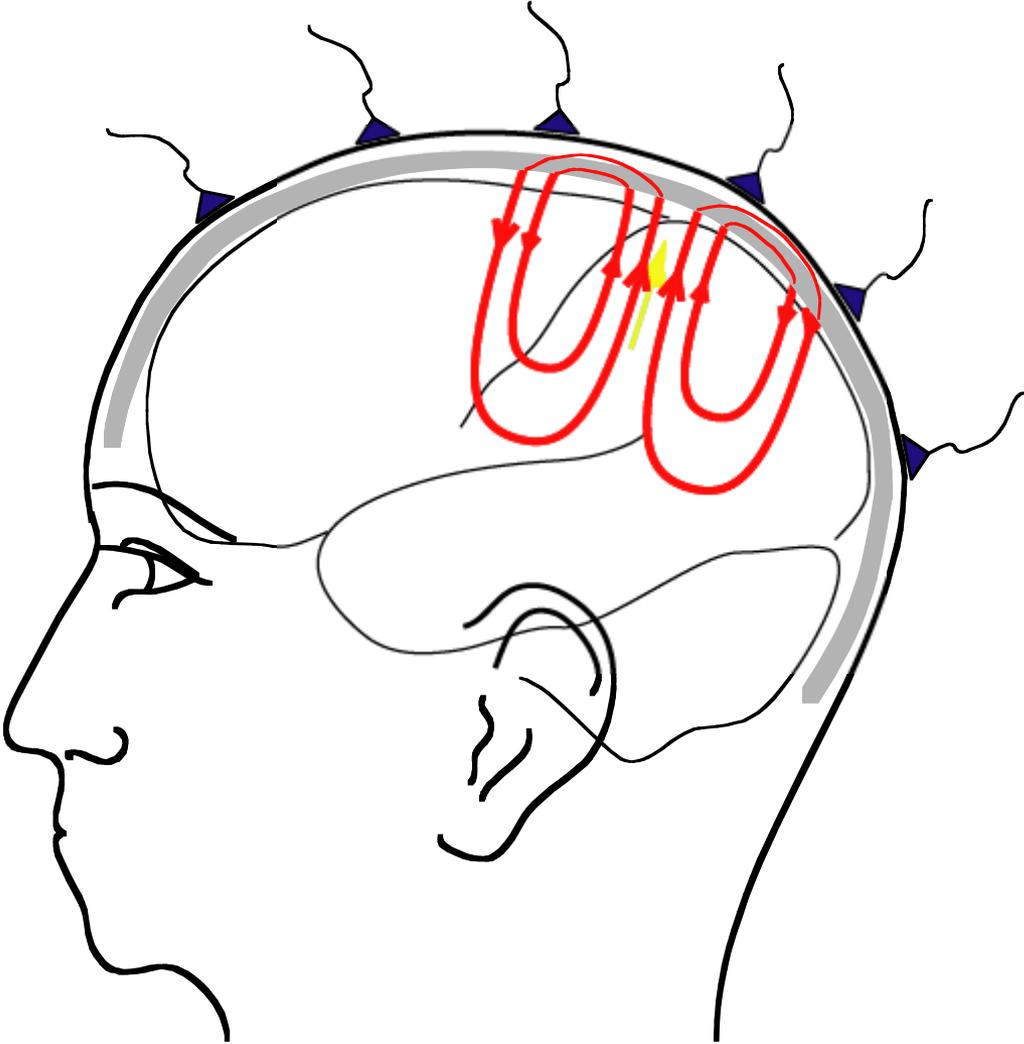
Linear equation for each node

approx.  $100 \times 100 \times 100 = 1.000.000$  linear equations  
just as many unknown potentials

Inject some current  $+I$  and  $-I$  at two of the nodes

Solve for unknown potential

# EEG volume conduction



# EEG volume conduction

Potential difference between electrodes  
corresponds to current flowing through skin

Only tiny fraction of current passes through skull

Therefore the model should describe the skull and  
skin **as accurately as possible**

# MEG volume conduction

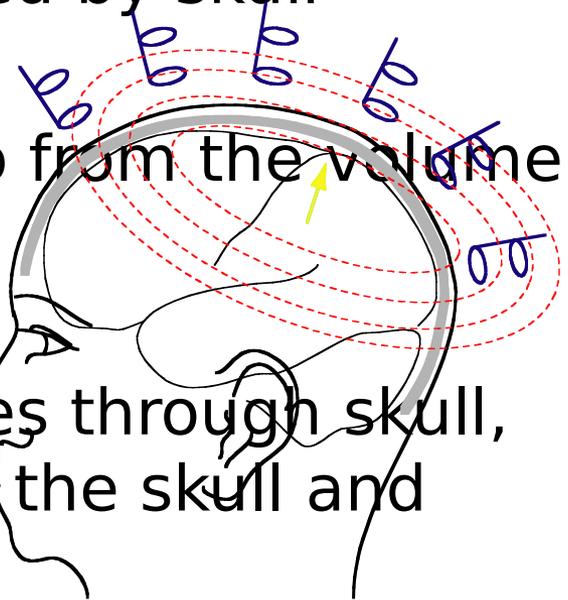
MEG measures magnetic field over the scalp



M distorted by skull

M it also from the volume

O passes through skull,  
ignore the skull and



# Practical differences between EEG and MEG

fixed sensor positions in MEG

flexible cap in EEG

MEG requires head size to be known in analysis  
using individual anatomical MRI  
position of sensors is accurately known

EEG requires the electrode positions to be known  
in analysis

# Obtaining geometrical data



\$\$\$

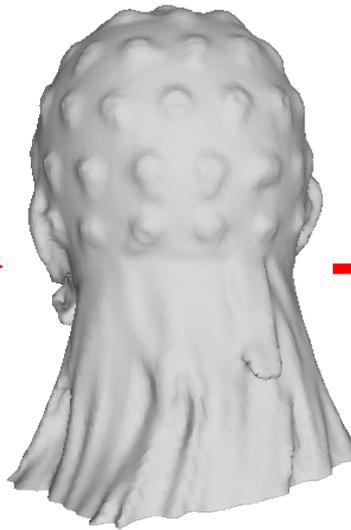


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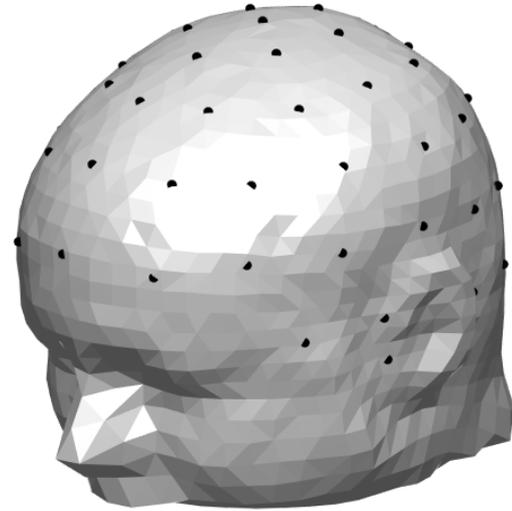
# 3D scanning instead of MRI



# 3D scanning - pipeline for EEG modelling

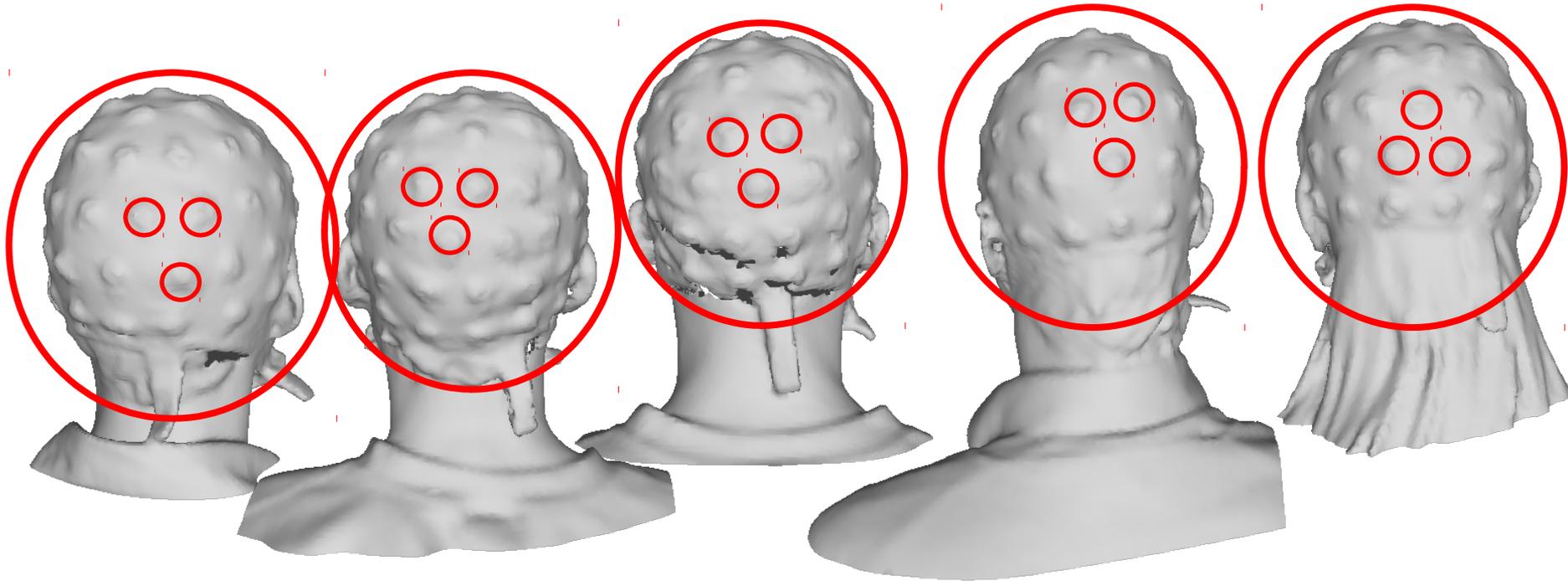


Surface scan



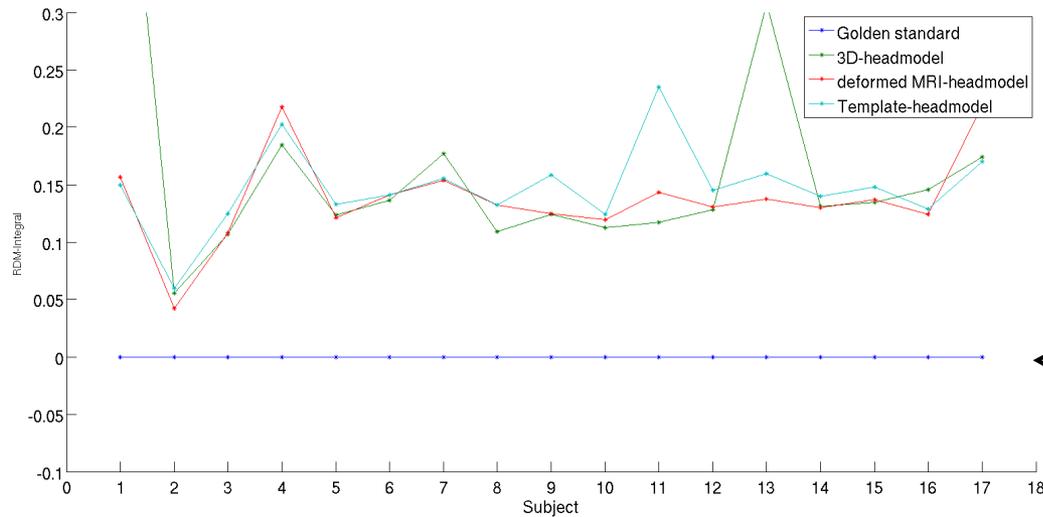
Individualised  
template

# 3D scanning



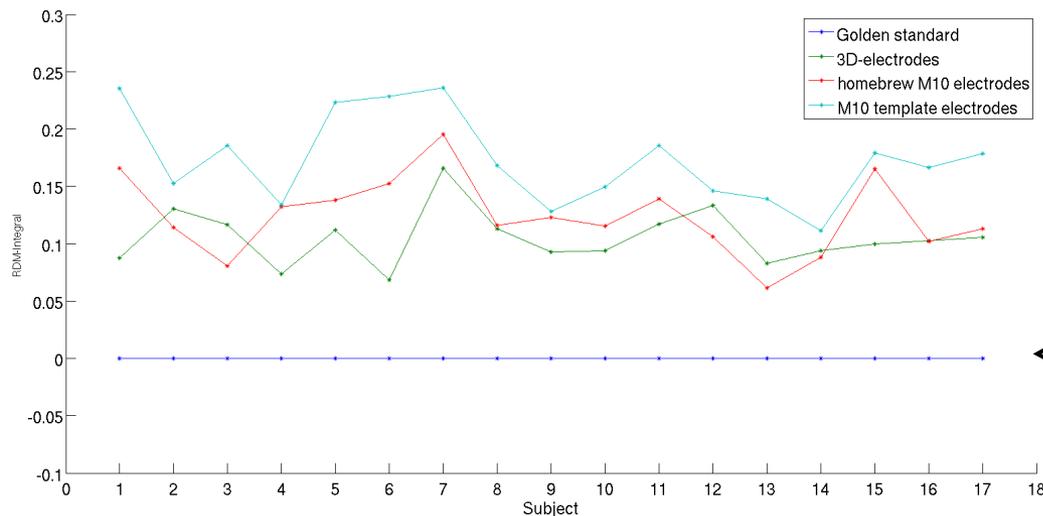
Homölle & Oostenveld  
in preparation

# 3D scanning - EEG source model accuracy



**comparing  
head models**

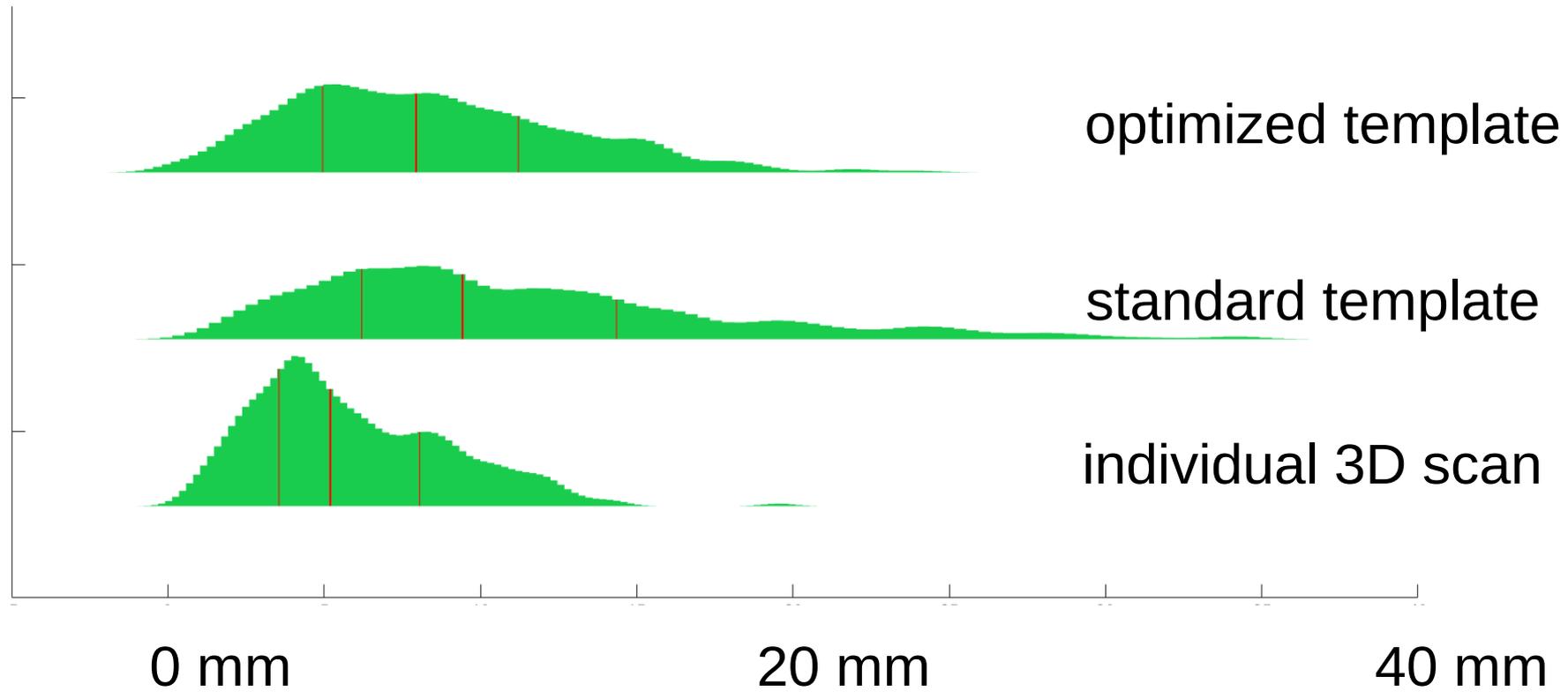
← MRI+polhemus



**comparing  
electrode locations**

← MRI+polhemus

# 3D scanning - Electrode position accuracy



# Forward modeling - summary

Using geometrical data

scalp, skull and brain tissue

locations at which MEG/EEG data is recorded

Measure geometrical data

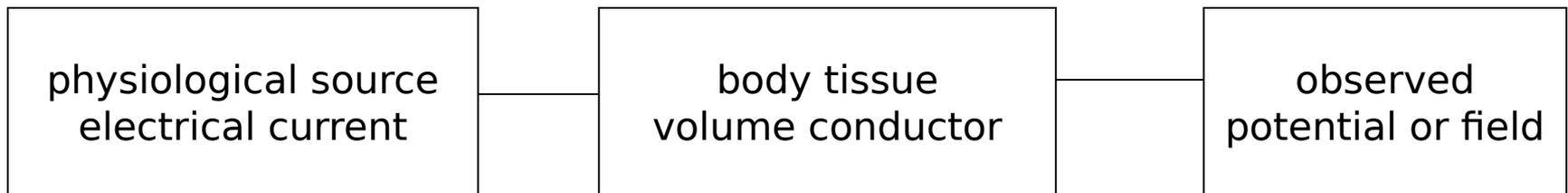
ideally with MRI and Polhemus

optionally with 3-D scanner

Mathematical volume conduction models

# Biophysical source modelling: overview

***forward model***



***inverse model***



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Source and volume conduction models  
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aligning sensors with anatomy

## **Source reconstruction**

equivalent dipole fitting  
distributed models  
scanning methods

Summary

# Source reconstruction – overview of methods

## Single and multiple dipole models

Minimize error between model and measured potential/field

## Distributed source models

Perfect fit of model to the measured potential/field

Additional constraint on source smoothness, power or amplitude

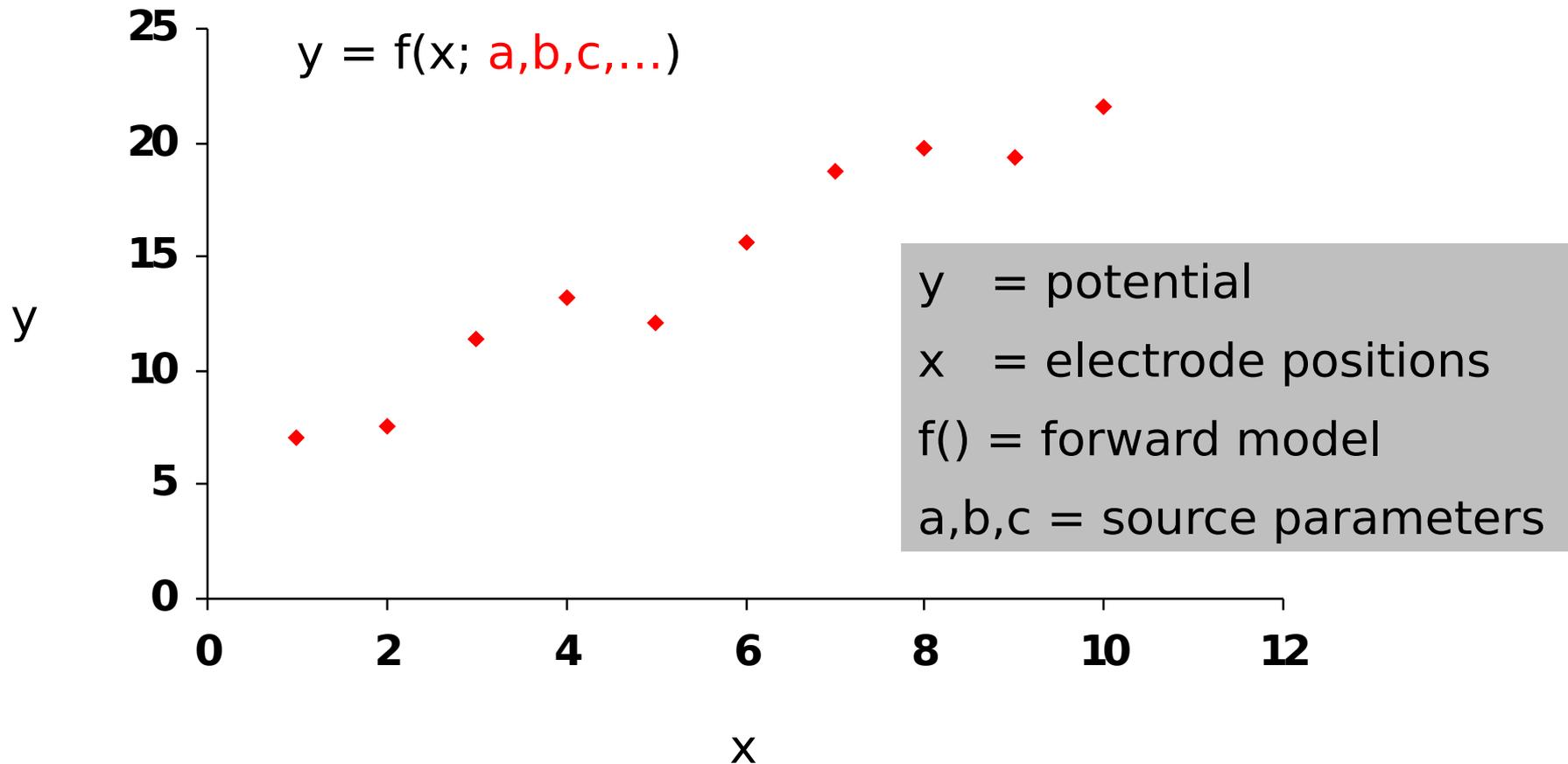
## Spatial filtering

Scan the whole brain with a single dipole and compute the filter output at every location

Beamforming (e.g. LCMV, SAM, DICS)

Multiple Signal Classification (MUSIC)

# Single or multiple dipole models - Parameter estimation



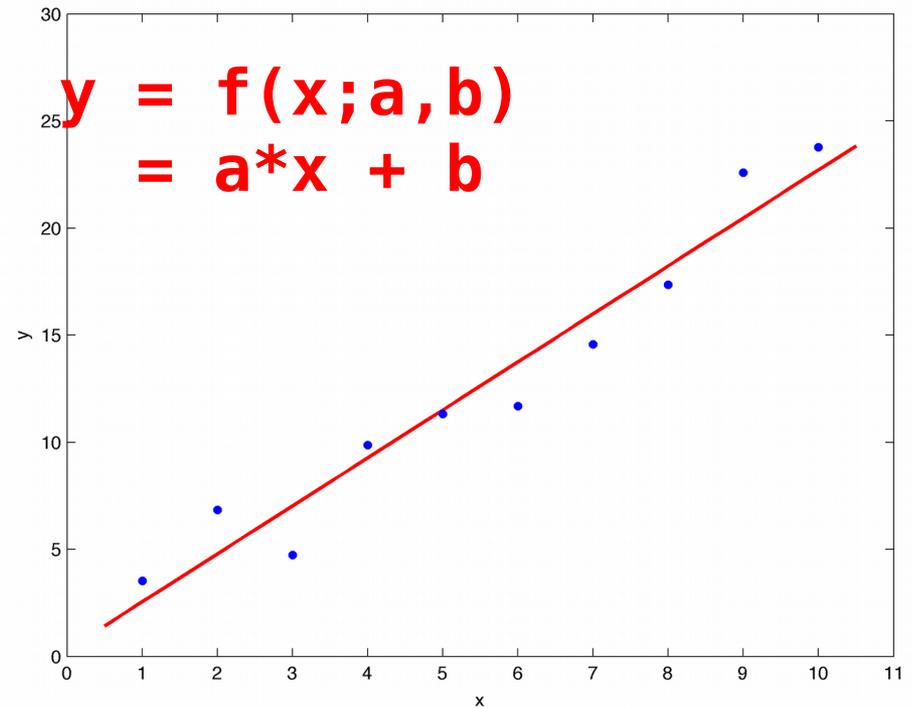
# Parameter estimation: dipole parameters

source model with  
few parameters

position  
orientation  
strength

compute the model  
data

minimize difference  
between actual and  
model data



## Non-linear parameters: grid search

One dimension, e.g. location along medial-lateral

100 possible locations

Two dimensions, e.g. med-lat + inf-sup

$100 \times 100 = 10.000$

Three dimensions

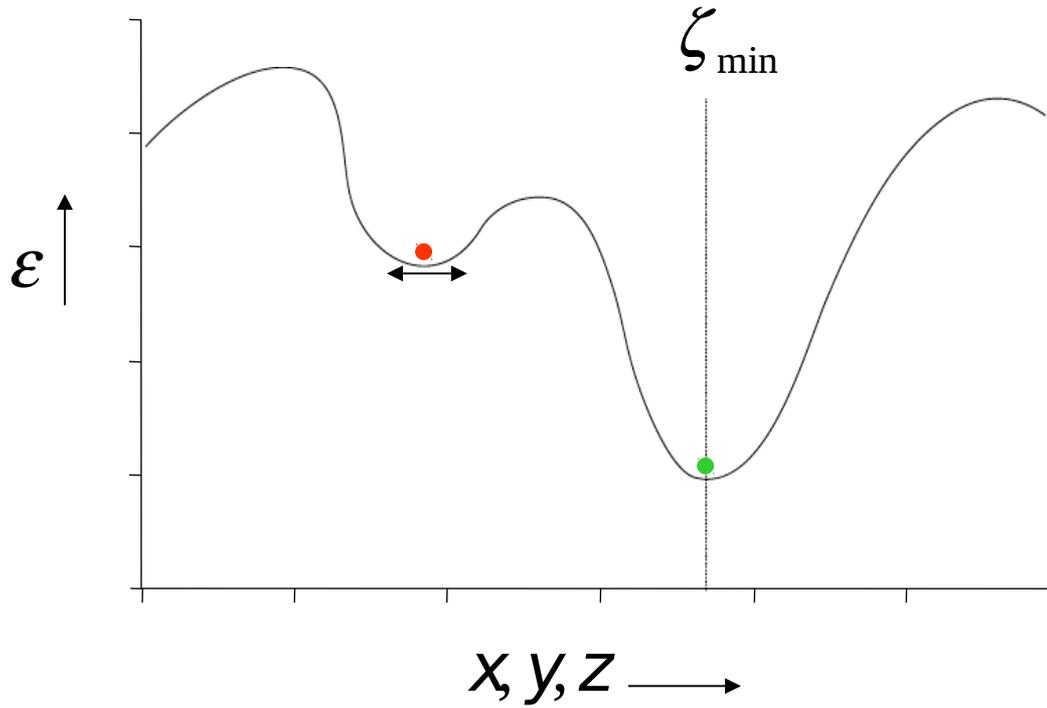
$100 \times 100 \times 100 = 1.000.000 = 10^6$

Two dipoles, each with three dimensions

$100 \times 100 \times 100 \times 100 \times 100 \times 100 = 10^{12}$

# Optimization of non-linear parameters

$$\text{error}(x, y, z) = \sum_{i=1}^N (Y_i(x, y, z) - V_i)^2 \Rightarrow \min_{x, y, z} (\text{error}(x, y, z))$$



# Single or multiple dipole models - Strategies

Single dipole:

scan the whole brain, followed by iterative optimization

Two dipoles:

scan with symmetric pair, use that as starting point for iterative optimization

More dipoles:

sequential dipole fitting

# Sequential dipole fitting: spread of cortical activity

Assume that activity starts “small”

explain earliest ERP component with single equivalent current dipole

Assume later activity to be more widespread

add ECDs to explain later ERP components

estimate position of new dipoles

re-estimate the activity of all dipoles

# Distributed source model

Position of the source is **not estimated** as such

Pre-defined grid (3D volume or on cortical sheet)

Strength is estimated

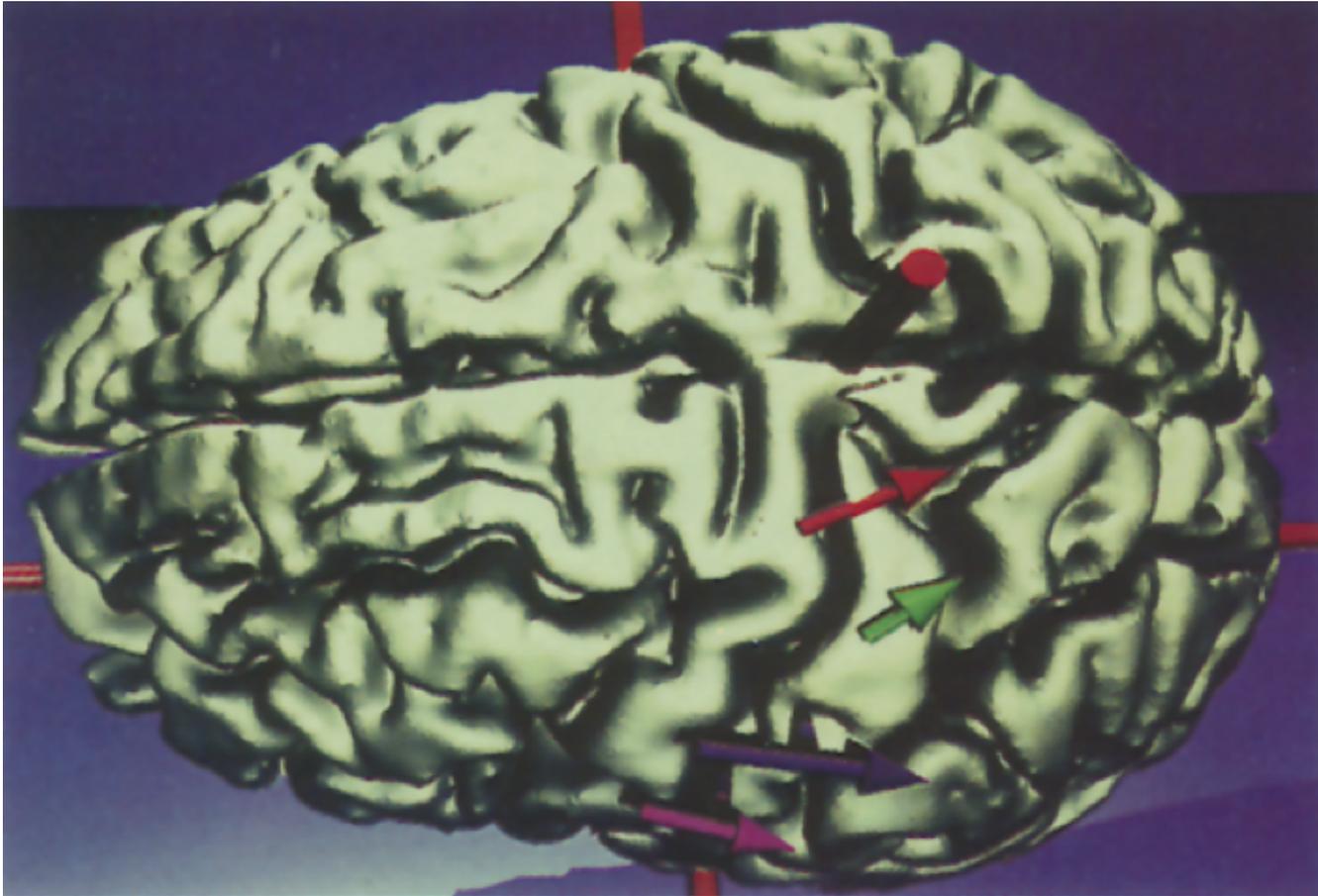
In principle easy to solve, however...

More “unknowns” (parameters) than “knowns”  
(measurements)

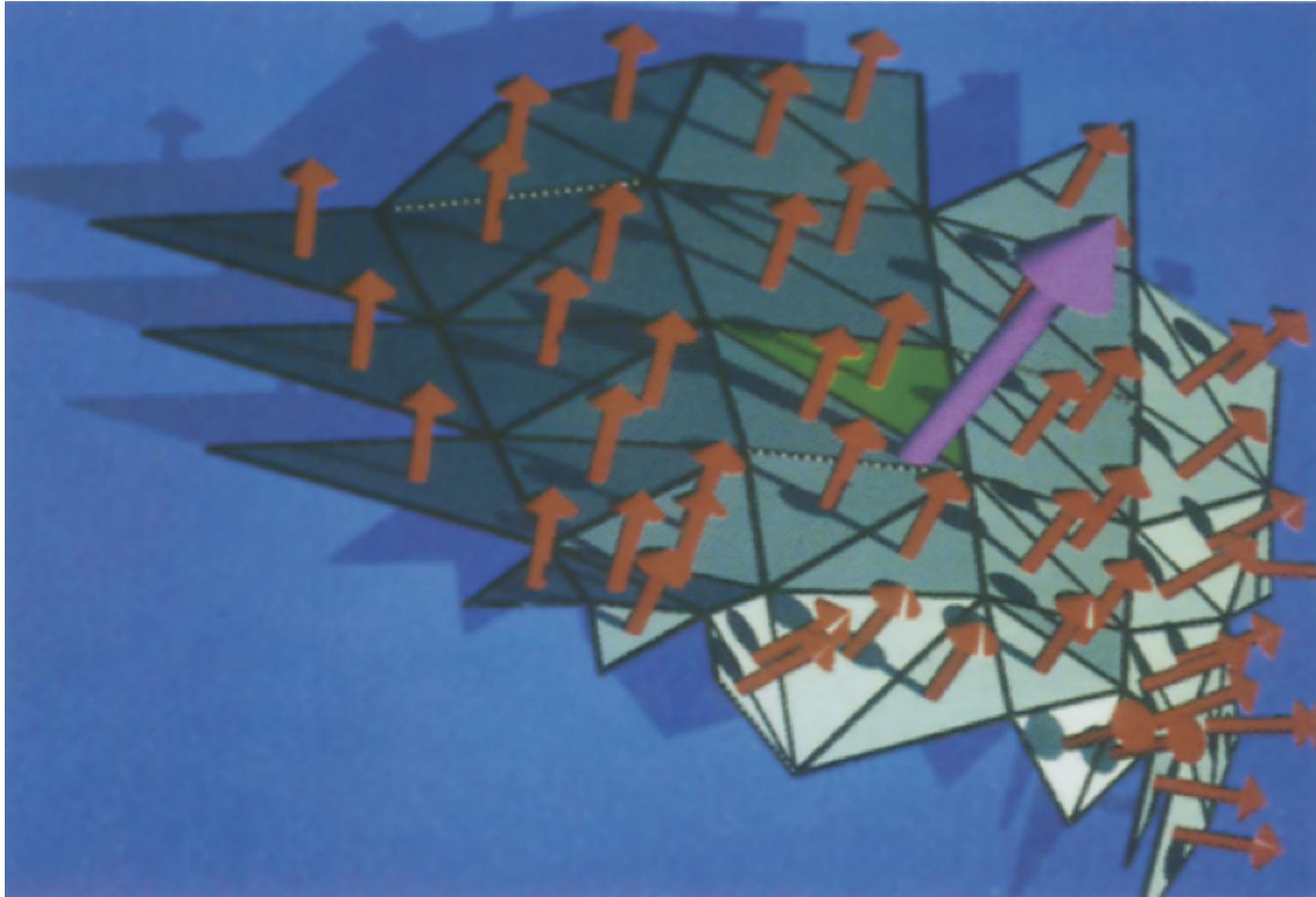
Infinite number of solutions can explain the data  
perfectly

Additional constraints required

# Distributed source model



# Distributed source model

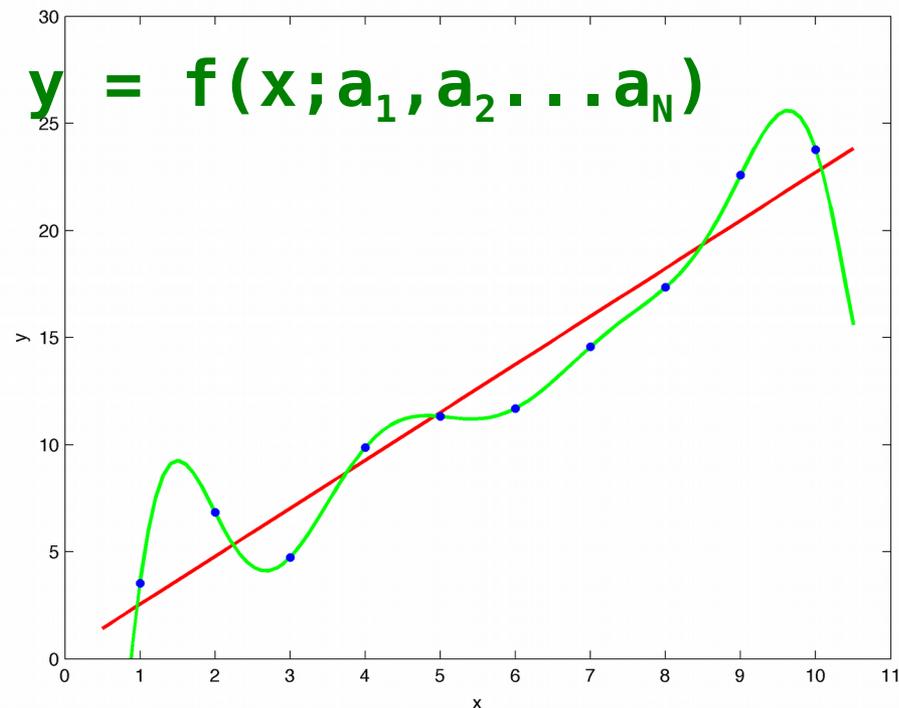


# Distributed source model: linear estimation

distributed source model  
with **many dipoles**  
throughout the whole  
brain

estimate the strength of  
all dipoles

data and noise can be  
perfectly explained



## Distributed source model: regularization

$$V = G \times q + \text{Noise}$$

$$\min_q \{ \|V - G \times q\|^2 \} = 0 \quad !!$$

Regularized linear estimation:

$$\rightarrow \min_q \{ \|V - G \times q\|^2 + \lambda \|D \times q\|^2 \}$$



mismatch with data



mismatch with prior  
assumptions

# Scanning methods

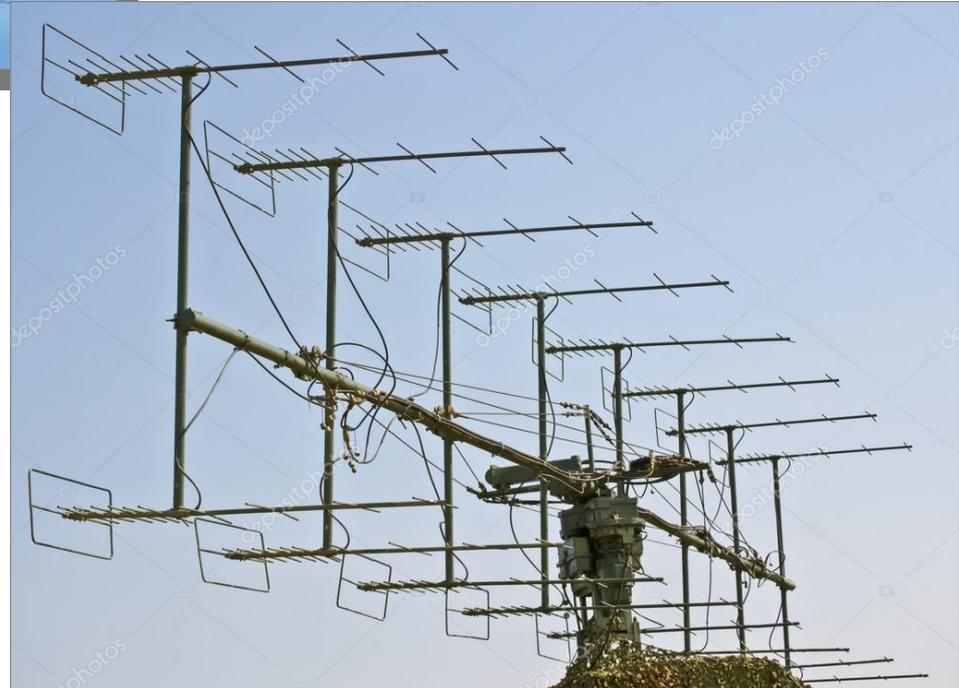
Position of the source is **not estimated** as such  
For each (possible) source position, an estimate of the activity is computed

Construct a “spatial filter”

No explicit assumptions about source constraints  
(implicit: single dipole)

Assumption that sources that contribute to the data should be uncorrelated

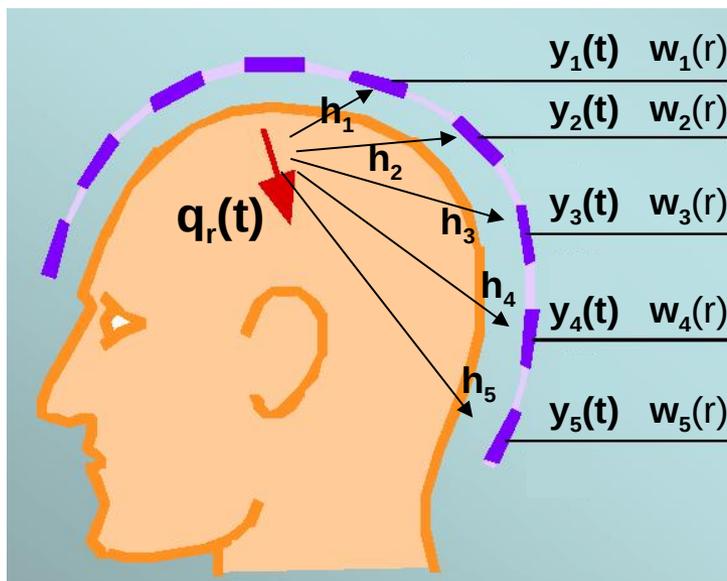
# Scanning with a beamformer filter



# Beamformer: the question

What is the activity of a source  $\mathbf{q}$ , at a location  $\mathbf{r}$ , given the data  $\mathbf{y}$ ?

We estimate  $\mathbf{q}$  with a spatial filter  $\mathbf{w}$



$$\hat{\mathbf{q}}_r(t) = \mathbf{w}(r)^\top \mathbf{y}(t)$$

# Summary 1

## Forward modelling

Required for the interpretation of scalp topographies  
Different methods with varying accuracy

## Inverse modelling

Estimate source location and timecourse from data

## Assumptions on source locations

Single or multiple point-like source  
Distributed source

## Assumptions on source and noise timecourse

Uncorrelated (and dipolar)

# Summary 2

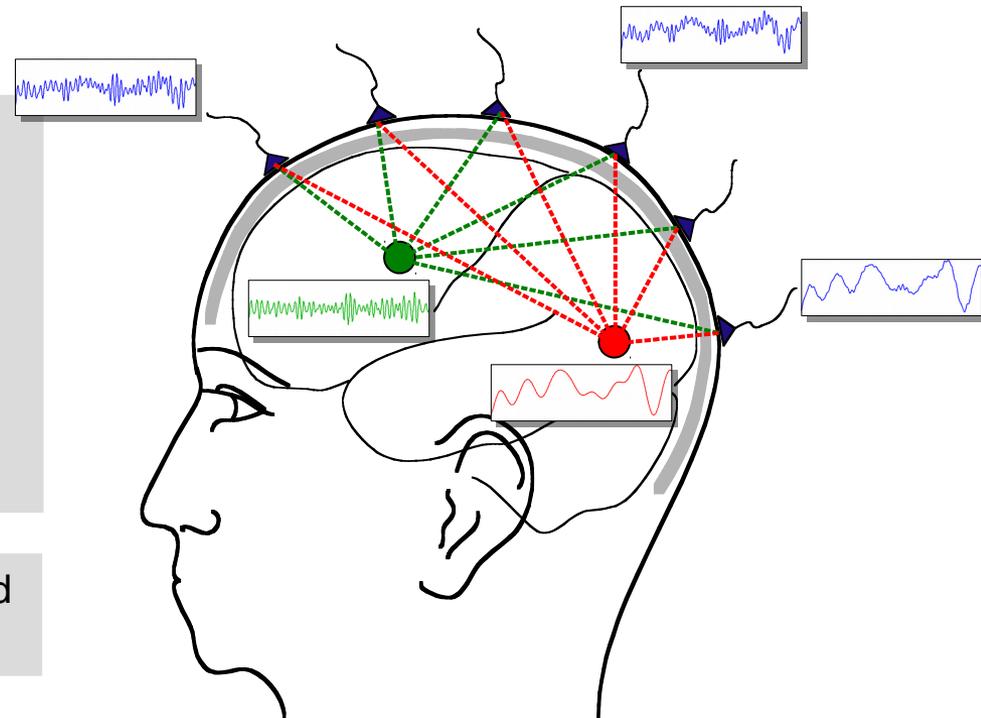
Source analysis is not only about the “where” but also about untangling the “what”, the “when” and the “how”

timecourse of activity  
-> ERP

spectral characteristics  
-> power spectrum

temporal changes in power  
-> time-frequency response (TFR)

spatial distribution of activity over the head  
-> source reconstruction



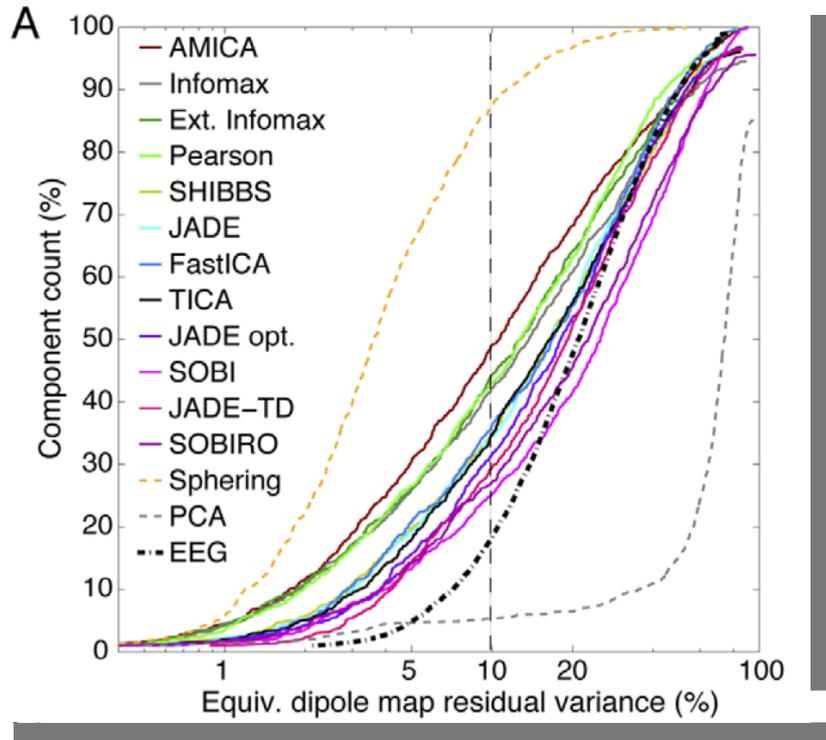
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# Independent components are dipolar



# Independent components are dipolar

